

# Research Data for the article “Mitigation of Nonlinear Effects in Optical Communications using Digital and Optical Techniques”

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## 1. Supplementary details for Figure 1:

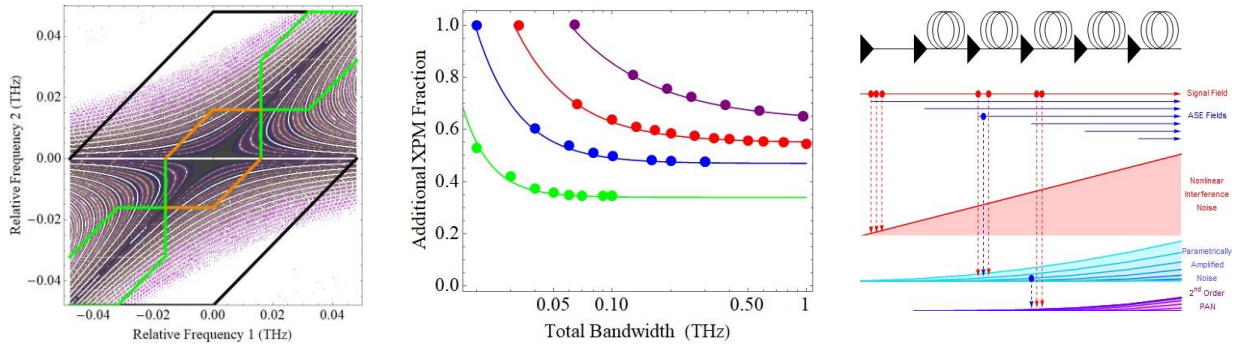


Fig. 1. (left) Four wave mixing efficiency (density plot) against frequency, showing integration bounds for self-phase modulation like terms (orange) cross-phase modulation like terms (green) and four wave mixing (black), (center) relative fraction of nonlinear noise from phase modulation-like terms as a function of WDM signal bandwidth for 10 (green) to 64 (purple) GHz channel bandwidths (right) illustration of the generation of nonlinear mixing products.

Figure 1 (left and center) present integration of the conventional FWM efficiency according to the approach in [5]. For figure 1 left, the integration limits for compensation of cross phase modulation are given by:

$$f_2^{\pm}(R) = \text{Min} \left( \left| \frac{f_1}{R} + \frac{1}{2} \right|, f_1 \right) R \pm \frac{R}{2}$$

Where  $f_1$  is relative frequency 1,  $f_2$  relative frequency 2 and R the symbol rate or WDM signal bandwidth. Figure 1 (centre) is calculated by diving integration of the FWM efficiency between  $f_2^-(R)$  and  $f_2^+(R)$  by the integration of the FWM efficiency between  $f_2^-(N.R)$  and  $f_2^+(N.R)$  where N is the number of channels considered. In this example the integration was carried out assuming an 80km span of standard single-mode fiber.

Coordinates of the points shown in Fig 1 (centre) are (to two significant figures):

10 GHz: {{0.02, 0.53}, {0.03, 0.42}, {0.04, 0.37}, {0.05, 0.36}, {0.06, 0.35}, {0.07, 0.35}, {0.09, 0.35}, {0.1, 0.35}, {0.1, 0.35}}

20 GHz: {{0.02, 1.0}, {0.04, 0.60}, {0.06, 0.54}, {0.08, 0.51}, {0.1, 0.50}, {0.2, 0.48}, {0.3, 0.48}, {0.3, 0.48}, {0.16, 0.48}}

33 GHz: {{0.033, 1.}, {0.066, 0.70}, {0.1, 0.64}, {0.13, 0.61}, {0.17, 0.60}, {0.2, 0.59}, {0.27, 0.57}, {0.33, 0.57}, {0.4, 0.56}, {0.5, 0.56}, {0.6, 0.55}, {0.77, 0.55}, {1., 0.55}}

64 GHz: {{0.064, 1.0}, {0.13, 0.81}, {0.26, 0.73}, {0.96, 0.65}, {0.96, 0.65}, {0.19, 0.76}, {0.38, 0.69}, {0.58, 0.67}}

Figure 1 right illustrates the length scaling rules reported in [1].

## 2. Supplementary details for Figure 2:

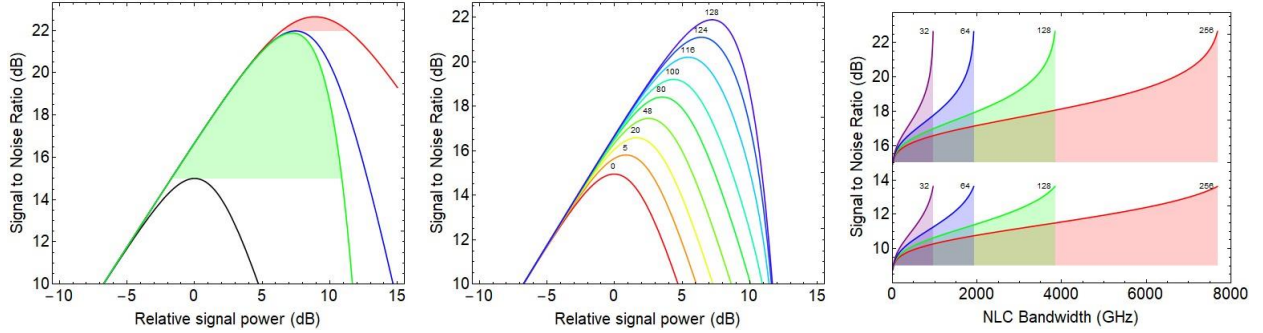


Fig. 2. Theoretical predictions of nonlinear compensation benefits showing (left) signal transmission limited by: black – inter signal nonlinearity, red – PNA, blue – second order PNA, green – all orders of PNA. (center) potential benefit of ideal nonlinearity compensation in a 128-channel system with a SNR before NLC of 15dB, and (right) potential SNR of 32 (purple), 64 (blue), 128 (green) and 256 (red) channel systems as a function of compensator bandwidth for a starting SNR of 9 (bottom) and 15 (top) dB.

Figure 2 is plotted for a generic system with 20 spans, and arbitrary nonlinear coefficient and an ASE noise spectral density selected to give a 15dB SNR without any compensation of nonlinear effects. Equations governing the curves are taken from [1], except for the “all-order” PNA, where the length scaling is adapted from [7]. For Figure 2 (centre) and Figure 2 (right) the proportion of residual inter-signal nonlinearity is simplifies to

$$1 - \frac{\text{Log} \left( R_c / B_0 \right)}{\text{Log} \left( N \cdot R / B_0 \right)}$$

Where  $R_c$  is the effective bandwidth of the nonlinearity compensation, and  $B_0$  a parameter reflecting the bandwidth of the first lobe of the FWM efficiency [5].

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#### 4. References for Figure 3.

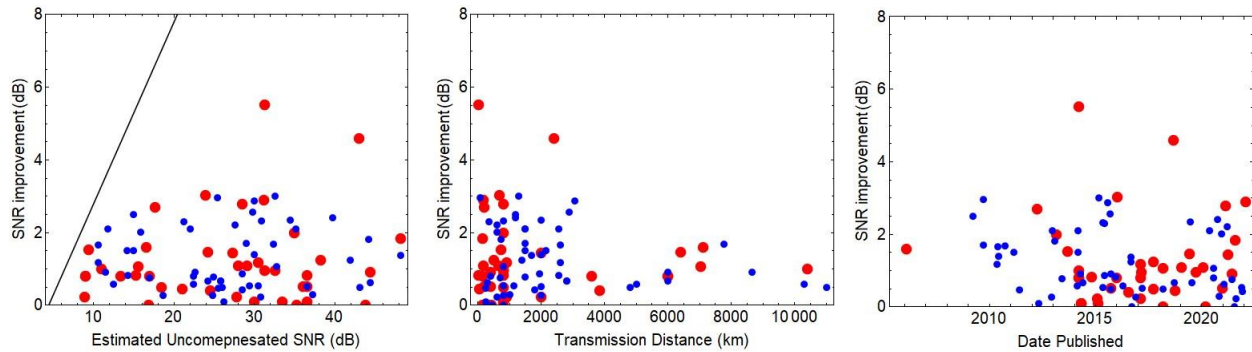


Fig. 3: Progress in digital (blue) and OPC-based (red) nonlinearity compensation.

For figure 3, results reported in each paper were converted to an equivalent SNR using the approach proposed in [1], except results reporting mutual information, where the SNR was taken assuming that the mutual information and SNR were related by Shannon's capacity formula.

##### 4.1. References for Compensation of Nonlinearity by Optical Phase Conjugation

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## **5. Funding**

This paper was funded in part by the EPSRC, grant numbers [EP/S003436/1](#), [EP/S016171/1](#), [EP/W002868/1](#) and [EP/R035342/1](#).